



**...day June 20XX – Morning/Afternoon**

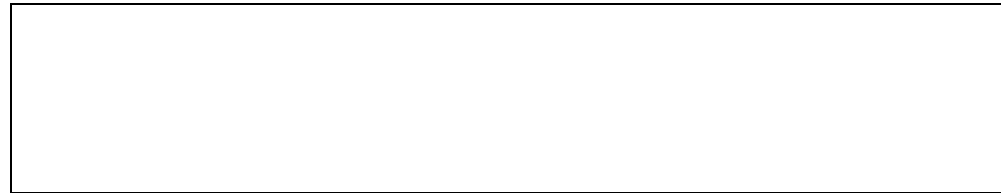
**A Level Further Mathematics A**

**Y540 Pure Core 1**

**SAMPLE MARK SCHEME**

**Duration:** 1 hour 30 minutes

**MAXIMUM MARK    75**



**This document consists of 16 pages**

## Text Instructions

## 1. Annotations and abbreviations

<b>Annotation in scoris</b>	<b>Meaning</b>
✓ and ✕	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
<b>Other abbreviations in mark scheme</b>	<b>Meaning</b>
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This question included the instruction: In this question you must show detailed reasoning.

**2. Subject-specific Marking Instructions for A Level Further Mathematics A**

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

**M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

**A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

**B**

Mark for a correct result or statement independent of Method marks.

**E**

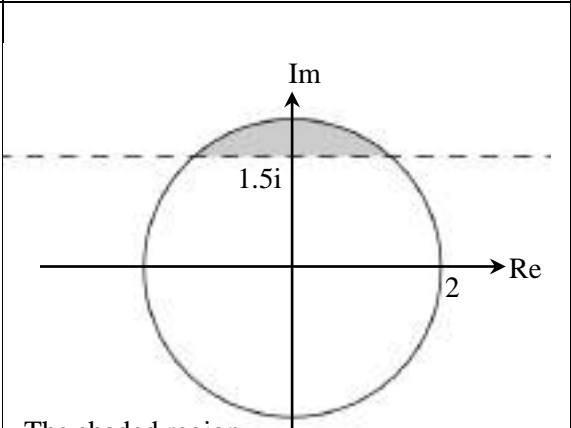
Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

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- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep\*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.  
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some papers. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question		Answer	Marks	AO	Guidance
1		$\frac{5}{2-4i} = \frac{5}{2-4i} \times \frac{2+4i}{2+4i} = \frac{10+20i}{20} = \frac{1}{2} + i$	<b>M1</b> <b>A1</b> [2]	<b>2.1</b> <b>1.1</b>	For multiplying numerator and denominator by $2+4i$ or multiplying $\frac{1}{2} + i$ by $2-4i$ Clear demonstration
2	(i)	<b>DR</b> $\alpha = 2+3i \Rightarrow \beta = 2-3i$ $\Rightarrow x^2 - 4x + 13 = 0$ is a quadratic factor $\Rightarrow f(x) = (x^2 - 4x + 13)(x^2 + 6x + 13)$	<b>B1</b> <b>M1</b> <b>M1</b> <b>A1</b> [4]	<b>2.2a</b> <b>1.1</b> <b>1.1</b> <b>1.1</b>	Attempt to create first quadratic Attempt to derive second quadratic Must come from $(x-\alpha)(x-\beta)$
2	(ii)	<b>DR</b> $\Rightarrow$ Roots are $2 \pm 3i, -3 \pm 2i$	<b>A1</b> [1]	<b>1.1</b>	Depends on <b>M2</b> awarded in part (i)
3		<b>DR</b> $r=0 \Rightarrow k = \frac{1}{8}$ $A = \frac{1}{2} \int_{-\frac{1}{8}\pi}^{\frac{1}{8}\pi} r^2 d\theta = \frac{1}{2} \int_{-\frac{1}{8}\pi}^{\frac{1}{8}\pi} (2\cos 4\theta)^2 d\theta$ $= 2 \int_{-\frac{1}{8}\pi}^{\frac{1}{8}\pi} \cos^2 4\theta d\theta$ $= \int_{-\frac{1}{8}\pi}^{\frac{1}{8}\pi} (1 + \cos 8\theta) d\theta = \left[ \theta + \frac{\sin 8\theta}{8} \right]_{-\frac{1}{8}\pi}^{\frac{1}{8}\pi}$ $= \left( \frac{1}{8}\pi + \frac{\sin \pi}{8} \right) - \left( -\frac{1}{8}\pi + \frac{\sin(-\pi)}{8} \right) = \frac{1}{4}\pi$	<b>B1</b> <b>M1</b> <b>A1</b> <b>A1</b> <b>M1</b> <b>A1</b> [6]	<b>2.2a</b> <b>3.1a</b> <b>1.1</b> <b>1.1</b> <b>3.1a</b> <b>1.1</b>	Limits not required Correct form to be integrated Correct indefinite integral Using correct limits Must show $f(\frac{1}{8}\pi) - f(-\frac{1}{8}\pi)$ Must be seen Must be seen <b>A0</b> for decimal answer

Question	Answer	Marks	AO	Guidance
4	 <p>The shaded region is the required locus</p>	<p><b>B1</b> <b>B1</b> <b>B1</b></p> <p>[3]</p>	<p><b>1.1</b> <b>1.1</b> <b>1.1</b></p>	<p>Circle centre 0, radius 2 Line parallel to <math>x</math> axis... Through 1.5i Correct shading with continuous arc and dashed line Must state which region is the required locus</p>
5 (i)	$\frac{d}{dx}(\sinh^{-1}(2x))$ $= \frac{1}{\sqrt{x^2 + (\frac{1}{2})^2}}$ $= \frac{1}{\sqrt{x^2 + (\frac{1}{2})^2}} \times \frac{2}{2} = \frac{2}{\sqrt{4x^2 + 1}}$	<p><b>M1</b> <b>E1</b></p> <p>[2]</p>	<p><b>1.1a</b> <b>2.1</b></p>	<p>Use formulae from formulae booklet AG At least one intermediate step must be seen <b>OR</b> <b>M1</b> <math>\sinh y = 2x</math> so <math>\frac{dy}{dx} \cosh y = 2</math> <b>E1</b> <math>\frac{dy}{dx} = \frac{2}{\cosh y} = \frac{2}{\sqrt{4x^2 + 1}}</math></p>
5 (ii)	$2 - 2x + x^2 = 1 + (x-1)^2$ $\Rightarrow \int \frac{1}{\sqrt{1+(x-1)^2}} dx = [\sinh^{-1}(x-1)] + c$	<p><b>B1</b> <b>M1</b> <b>A1</b></p> <p>[3]</p>	<p><b>3.1a</b> <b>1.1</b> <b>1.1</b></p>	<p>Complete square soi Use correct form oe</p>

Question	Answer	Marks	AO	Guidance	
6	$\alpha + \beta + \gamma = -2, \alpha\beta + \beta\gamma + \gamma\alpha = 1,$ $\alpha\beta\gamma = -3$ $p = -(\alpha\beta + \beta\gamma + \gamma\alpha) = -1$ $q = \alpha\beta\beta\gamma + \beta\gamma\gamma\alpha + \gamma\alpha\alpha\beta$ $= \alpha\beta\gamma(\alpha + \beta + \gamma) = 6$ $r = -\alpha\beta\beta\gamma\gamma\alpha = -9$	<b>B1</b>  <b>B1</b>  <b>M1</b> <b>A1</b>  <b>A1</b>  <b>[5]</b>	<b>1.1</b>  <b>1.1</b>  <b>2.1</b> <b>1.1</b>  <b>1.1</b>	soi  Manipulation of roots	
7 (i)	$\mathbf{n} = \begin{pmatrix} 1 \\ 2 \\ -3 \end{pmatrix} \times \begin{pmatrix} 2 \\ -1 \\ 4 \end{pmatrix} = \begin{pmatrix} 5 \\ -10 \\ -5 \end{pmatrix}$ $\mathbf{b} - \mathbf{a} = \begin{pmatrix} 4 \\ -2 \\ 7 \end{pmatrix} - \begin{pmatrix} 3 \\ 5 \\ -2 \end{pmatrix} = \begin{pmatrix} 1 \\ -7 \\ 9 \end{pmatrix}$ <p>Shortest distance is given by</p> $D = \frac{ (\mathbf{b} - \mathbf{a}) \cdot \mathbf{n} }{ \mathbf{n} } = \frac{\left  \begin{pmatrix} 1 \\ -7 \\ 9 \end{pmatrix} \cdot \begin{pmatrix} 5 \\ -10 \\ -5 \end{pmatrix} \right }{\sqrt{150}}$ $= \sqrt{6}$	<b>M1</b> <b>A1</b>  <b>B1</b>    <b>M1</b>    <b>A1</b>  <b>[5]</b>	<b>1.1a</b> <b>1.1</b>  <b>1.1</b>    <b>1.2</b>    <b>1.1</b>	Finding a mutual perpendicular  Any vector between the lines  Using formula from the formula booklet  Or any other valid method	
7 (ii)	$x - 2y - z = -5$	<b>M1</b>  <b>A1</b>  <b>[2]</b>	<b>3.1a</b>  <b>1.1</b>	Using their mutual perpendicular from part (i) oe	

Question		Answer	Marks	AO	Guidance	
8	(i)	$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 1 & 1 & 1 \\ 2 & 4 & 5 \\ 7 & 11 & 12 \end{pmatrix}^{-1} \begin{pmatrix} 3 \\ 9 \\ 20 \end{pmatrix}$ $x = 5, y = -9, z = 7$	M1	1.2	BC or in vector form	<b>OR</b> elimination method <b>M1</b> reduce to two equations in two unknowns
			A1 [2]	1.1		
8	(ii)	$\mathbf{M} = \begin{pmatrix} 1 & 1 & 1 \\ 2 & 4 & 5 \\ 7 & 11 & p \end{pmatrix}$ $\text{Det } \mathbf{M} = 4p + 35 + 22 - 28 - 2p - 55$ <p><math>\mathbf{M}</math> is singular, so <math>2p - 26 = 0</math></p> $\Rightarrow p = 13$ <p>The third equation must be a linear combination of the first two</p> $\alpha + 2\beta = 7, \alpha + 4\beta = 11, \alpha + 5\beta = 13$ $\Rightarrow \alpha = 3, \beta = 2$ $3\alpha + 9\beta = k \Rightarrow k = 27$	M1	1.1	calculating det $\mathbf{M}$	<b>OR</b> <b>M1</b> state that singular matrix requires each row to be a combination of the other two  <b>M1</b> state that $R_3 = 3R_1 + 2R_2$ or equivalent <b>A1</b> conclude that $p = 13$
			M1	2.1	setting their $2p - 26$ equal to 0 and solving	
			A1	1.1	conclude that $p = 13$	
			E1	2.2a	Deducing $R_3 = 3R_1 + 2R_2$	
			M1	3.1a		
			A1 [6]	1.1	27 from correct reasoning	



Question			Answer	Marks	AO	Guidance
9			<p>Formula is true for <math>n=1</math> since <math>\frac{1}{5^1} = \frac{1}{5}</math> and</p> $\frac{5-4 \times 1}{5} = \frac{1}{5}$ <p>Assume that the formula is true for <math>n=k</math></p> <p>Then <math>\sum_{r=1}^{k+1} \frac{5-4r}{5} = \frac{k}{5^k} + \frac{5-4(k+1)}{5^{k+1}}</math></p> $= \frac{5k+5-4(k+1)}{5^{k+1}}$ $= \frac{k+1}{5^{k+1}}$ <p>So if true for <math>n=k</math> then true also for <math>n=k+1</math></p> <p>So true generally</p>	<p><b>B1</b></p> <p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>E1</b></p> <p>[5]</p>	<p><b>2.5</b></p> <p><b>3.1a</b></p> <p><b>2.1</b></p> <p><b>2.2a</b></p> <p><b>2.4</b></p>	<p>Must include an arithmetic justification</p> <p>Add extra term</p> <p>Manipulate</p> <p>Needs conclusion</p>
10	(i)	(a)	All roots satisfy $ z^5  = a^5 \Rightarrow  z  = a$	<p><b>E1</b></p> <p>[1]</p>	<b>2.2a</b>	Clear justification that all points are equidistant from $O$
10	(i)	(b)	<p>All points are distance <math>a</math> from <math>O</math></p> <p>Each root of the form <math>a \operatorname{cis} \left( \frac{2k\pi}{5} \right)</math> hence</p> <p>spaced at angular intervals of <math>\frac{2\pi}{5}</math> around this circle</p>	<p><b>B1</b></p> <p><b>E1</b></p> <p>[2]</p>	<b>1.1</b>  <b>2.4</b>	Using the answer to part (b)

Question			Answer	Marks	AO	Guidance
10	(i)	(c)	$\arg\left(b \times e^{\frac{2\pi i}{5}}\right) = \arg(b) + \arg\left(e^{\frac{2\pi i}{5}}\right)$ $= \frac{4}{5}\pi = \arg(c)$	E1 [1]	2.2a	Multiplying any complex number by $e^{\frac{2i\pi}{5}}$ rotates it through an angle of $\frac{2\pi}{5}$ , so $b \rightarrow c$
10	(i)	(d)	$b^* = \text{cis}\left(\frac{2\pi}{5}\right)^* = \text{cis}\left(\frac{-2\pi}{5}\right) = \text{cis}\left(\frac{8\pi}{5}\right) = e$	E1 [1]	2.4	Or by noting that complex roots of a real polynomial occur in conjugate pairs (the pairing is obvious)
10	(i)	(e)	$a, b, c, d$ and $e$ are the roots of $z^5 - a^5 = 0$ so sum of $a, b, c, d$ and $e$ is $-\frac{0}{1} = 0$	M1 E1 [2]	2.1 1.1	Accept any complete justification
10	(ii)		All roots of equal magnitude $a \cos \frac{\pi}{5}$ All roots spaced at angles of $\frac{2\pi}{5}$ $r$ is negative real root $\Rightarrow z^5 + (a \cos \frac{\pi}{5})^5 = 0$	M1 B1 A1 [3]	3.1a 3.1a 2.2a	From any sensible right-angled triangle Must justify equally spread arguments Allow correct eqn. from 1 <sup>st</sup> M1 only

Question		Answer	Marks	AO	Guidance
11	(i)	$\frac{d}{dt} \left( 0.5 \frac{dm}{dt} + m \right) = k(80 - m)$ $0.5 \frac{d^2m}{dt^2} + \frac{dm}{dt} = k(80 - m)$ $\Rightarrow \frac{d^2m}{dt^2} + 2 \frac{dm}{dt} = 2k(80 - m)$ $\Rightarrow \frac{d^2m}{dt^2} + 2 \frac{dm}{dt} + 2km = 160k$	<b>B1</b>	<b>3.3</b>	Translate the given context into a correct mathematical model
			<b>E1</b>	<b>2.1</b>	AG
			[2]		
11	(ii)	$\frac{d^2m}{dt^2} + 2 \frac{dm}{dt} + 2km = 160k$ $\Rightarrow \text{A.E. } n^2 + 2n + 2k = 0$ $\Rightarrow n = \frac{-2 \pm \sqrt{4 - 8k}}{2} = -1 \pm \sqrt{1 - 2k}$ <p>CF in the form <math>A \cos 2t + B \sin 2t \Rightarrow</math>  <math>1 - 2k &lt; 0</math>  so <math>\sqrt{2k - 1} = 2 \Rightarrow k = \frac{5}{2}</math>  <math>\lambda = -1</math></p>	<b>M1</b>	<b>1.1</b>	For auxiliary equation
			<b>A1</b>	<b>1.1</b>	Need not be simplified
			<b>E1</b>	<b>2.2a</b>	AG
			<b>A1ft</b>	<b>1.1</b>	Follow through their auxiliary equation
			[4]		Or complete the square

Question		Answer	Marks	AO	Guidance	
11	(iii)	$\frac{d^2m}{dt^2} + 2\frac{dm}{dt} + 5m = 400$ <p>P.I. Try <math>m = \mu \Rightarrow \frac{dm}{dt} = \frac{d^2m}{dt^2} = 0</math></p> <p>Substituting <math>\Rightarrow 5\mu = 400 \Rightarrow \mu = 80</math></p> <p><math>\Rightarrow</math> G.S. <math>m = e^{-t}(A \cos 2t + B \sin 2t) + 80</math></p> <p><math>m = 0</math> when <math>t = 0</math></p> <p><math>\Rightarrow A = -80</math></p> <p><math>\frac{dm}{dt} = 160</math> when <math>t = 0</math></p> <p><math>\frac{dm}{dt} = -e^{-t}(A \cos 2t + B \sin 2t) + 2e^{-t}(-A \sin 2t + B \cos 2t)</math></p> <p><math>= 160</math> when <math>t = 0</math></p> <p><math>\Rightarrow -A + 2B = 160 \Rightarrow B = 40</math></p> <p><math>\Rightarrow m = e^{-t}(40 \sin 2t - 80 \cos 2t) + 80</math></p>	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p>[7]</p>	<p><b>3.1a</b></p> <p><b>1.1</b></p> <p><b>3.3</b></p> <p><b>1.1</b></p> <p><b>3.3</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p>	<p>Correct Particular Integral and substituting</p> <p>General Solution including correct <math>\mu</math></p> <p>Translate the given context into an initial condition to find <math>A</math></p> <p>Translate the given context into an initial condition to find <math>B</math></p> <p>Differentiation and substitution</p> <p>Final answer stated</p>	<p>Award first two marks if GS stated correctly</p>
11	(iv)	As $t \rightarrow \infty$ , $m \rightarrow 80$	<p><b>B1</b></p> <p>[1]</p>	<b>3.4</b>		
11	(v)	E.g. There is a limiting process here. According to the model the mass of the crate is only displayed after infinite time	<p><b>B1</b></p> <p>[1]</p>	<b>3.5b</b>		

Question			Answer	Marks	AO	Guidance	
11	(vi)	(a)	$m = e^{-t}(40\sin 2t - 80\cos 2t) + 80$ $\Rightarrow \frac{dm}{dt} = e^{-t}(160\cos 2t + 120\sin 2t) = 0$ ... when $t = 1.107 \Rightarrow m = 106$	<b>M1</b>  <b>A1</b>  <b>[2]</b>	<b>3.1b</b>  <b>3.4</b>	Differentiation, FT their expression from part (iii)  Set = 0 and solve BC, may be implied by 106	<b>OR</b> By graphical calculator <b>M1</b> draw $m = f(t)$ <b>A1</b> find value of $m$ at the first maximum
11	(vi)	(b)	This is the maximum mass displayed (to 3 sf)	<b>E1</b>  <b>[1]</b>	<b>3.2a</b>	Must state that this is the maximum value	
11	(vii)		e.g. $\frac{d^2m}{dt^2} + 2\frac{dm}{dt} + 5m = 500$	<b>E1</b>  <b>[1]</b>	<b>3.5c</b>	Any differential equation of the form $\frac{d^2m}{dt^2} + 2\frac{dm}{dt} + am = b$ with $\frac{b}{a} = 100$	Accept any sensible suggestion

## Assessment Objectives (AO) Grid

Question	AO1	AO2	AO3(PS)	AO3(M)	Total
1	1	1	0	0	2
2(i)	3	1	0	0	4
2(ii)	1	0	0	0	1
3	3	1	2	0	6
4	3	0	0	0	3
5(i)	1	1	0	0	2
5(ii)	2	0	1	0	3
6	4	1	0	0	5
7(i)	5	0	0	0	5
7(ii)	1	0	1	0	2
8(i)	2	0	0	0	2
8(ii)	3	2	1	0	6
9	0	4	1	0	5
10(i)(a)	0	1	0	0	1
10(i)(b)	1	1	0	0	2
10(i)(c)	0	1	0	0	1
10(i)(d)	0	1	0	0	1
10(i)(e)	1	1	0	0	2
10(ii)	0	1	2	0	3
11(i)	0	1	0	1	2
11(ii)	3	1	0	0	4
11(iii)	4	0	1	2	7
11(iv)	0	0	0	1	1
11(v)	0	0	0	1	1
11(vi)(a)	0	0	1	1	2
11(vi)(b)	0	0	1	0	1
11(vii)	0	0	0	1	1
<b>Totals</b>	<b>38</b>	<b>19</b>	<b>11</b>	<b>7</b>	<b>75</b>

PS = Problem Solving

M = Modelling

Summary of Updates

Date	Version	Change
October 2019	2	Amendments to the front cover rubric instructions to candidates

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## A Level Further Mathematics A

### Y540 Pure Core 1

Printed Answer Booklet

Version 2

## Date – Morning/Afternoon

Time allowed: 1 hour 30 minutes

**You must have:**

- Question Paper Y540 (inserted)
- Formulae A Level Further Mathematics A

**You may use:**

- a scientific or graphical calculator



First name

Last name

Centre  
number

Candidate  
number

### INSTRUCTIONS

- The Question Paper will be found inside the Printed Answer Booklet.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- **Write your answer to each question in the space provided in the Printed Answer Booklet.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question.
- The acceleration due to gravity is denoted by  $g \text{ m s}^{-2}$ . Unless otherwise instructed, when a numerical value is needed, use  $g = 9.8$

### INFORMATION

- **You are reminded of the need for clear presentation in your answers.**
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **8** pages.

<b>1</b>	
<b>2(i)</b>	
<b>2(ii)</b>	

<b>3</b>	

<p>4</p>	
<p>5(i)</p>	
<p>5(ii)</p>	

**6**


**7(i)**


(answer space continued on next page)

<b>7(i) (continued)</b>	
<b>7(ii)</b>	

**8(i)**


**8(ii)**


<b>9</b>	
<hr/>	
<b>10(i)(a)</b>	
<hr/>	
<b>10(i)(b)</b>	



<b>10(i)(c)</b>	
<b>10(i)(d)</b>	
<b>10(i)(e)</b>	
<b>10(ii)</b>	

<b>11(i)</b>	
<b>11(ii)</b>	

<b>11(iii)</b>	

<b>11(iv)</b>	
<b>11(v)</b>	
<b>11(vi)(a)</b>	
<b>11(vi)(b)</b>	
<b>11(vii)</b>	

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